

# From single cells to intricate multi-cell interactions in blood flow

Dmitry A. Fedosov

Institute of Complex Systems and Institute for Advanced Simulation,  
Forschungszentrum Jülich, 52425 Jülich, Germany

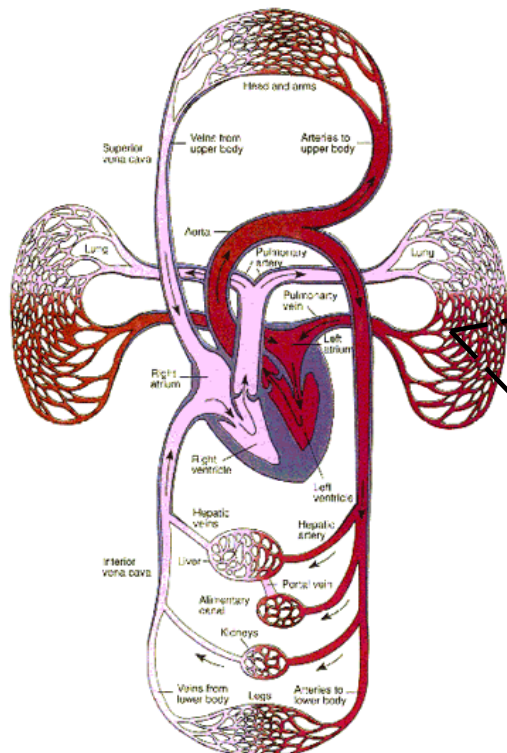
# Forschungszentrum Jülich



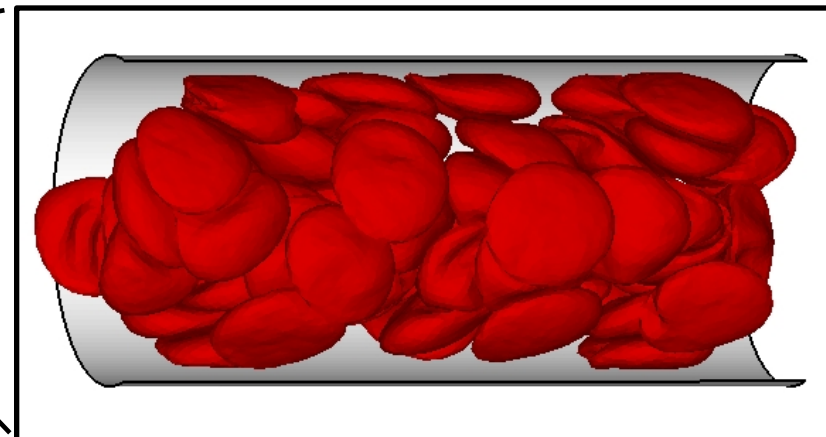
- One of the largest research centers in Germany with nearly 5000 employees
- Research includes energy, health, materials, etc.

# Blood flow

- Blood transports oxygen and nutrients to cells of the body, removes waste products, and circulates molecules and cells which mediate various organism functions
- Abnormal blood flow and rheology is often associated with some blood disorders and diseases such as hypertension, anemia, malaria, and thrombosis

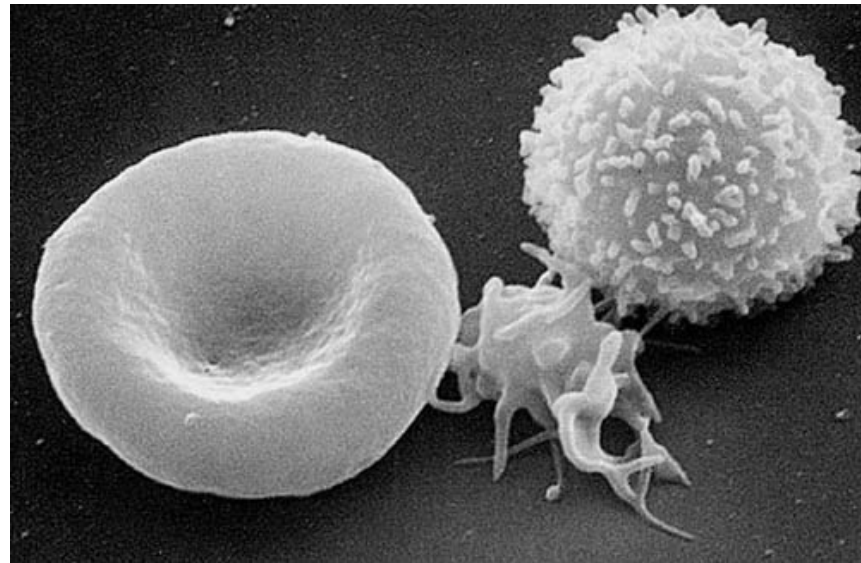
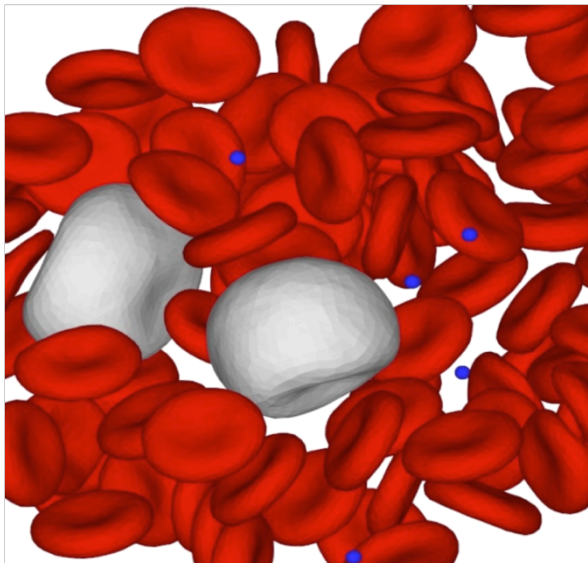


- Biomedical and bioengineering applications: blood substitutes, blood flow assisting devices, lab-on-a-chip, and drug delivery



# Blood

- ❖ Adults have about 5 liters of blood formed by erythrocytes (red blood cells) - 45%, leukocytes (white blood cells) - 0.7%, blood plasma – 54%, thrombocytes (platelets)
- ❖ Blood plasma consists of about 92% water, 8% proteins and other materials
- ❖ One microliter of blood has about 4-6 million RBCs, 4-10 thousand WBCs, and half a million platelets



# Modeling fluid flow

## Incompressible Navier-Stokes equation

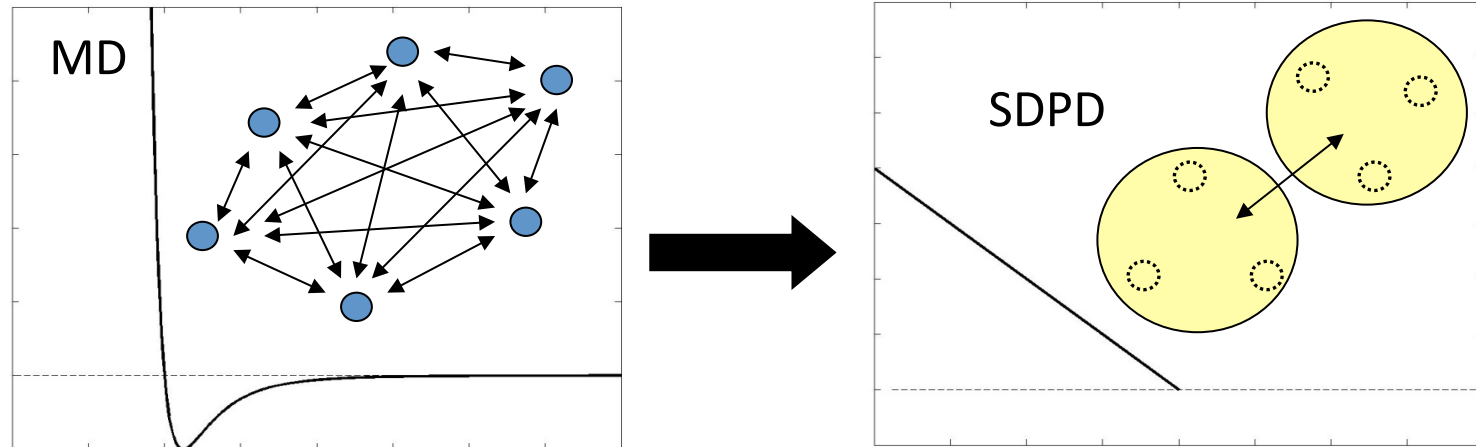
$$\frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \nabla) \vec{u} = -\frac{1}{\rho} \nabla p + \nu \nabla^2 \vec{u}$$

$$\nabla \cdot \vec{u} = 0$$

There exist different methods for solving NS equation:

- Eulerian discretization – finite difference, finite volume, finite element, etc.
- Lagrangian discretization – particle-based methods, etc.

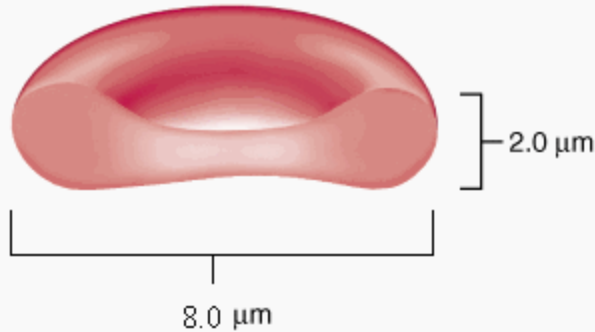
# Smoothed dissipative particle dynamics method



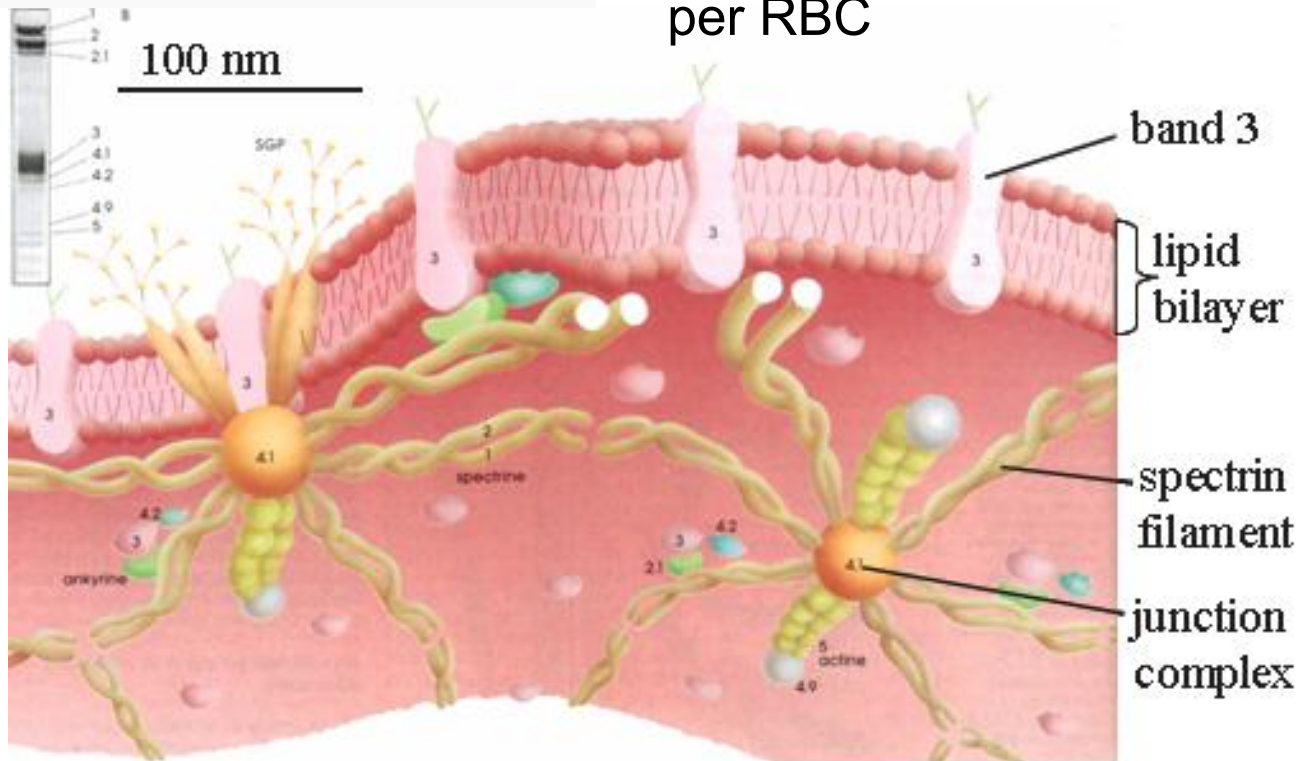
- SDPD is a mesoscopic particle-based hydrodynamics method
- Particles interact through a simple pair-wise potential
- The time evolution of positions and velocities are given by

$$d\mathbf{r}_i = \mathbf{v}_i dt \quad d\mathbf{v}_i = \mathbf{F}_i dt$$

# Red blood cells



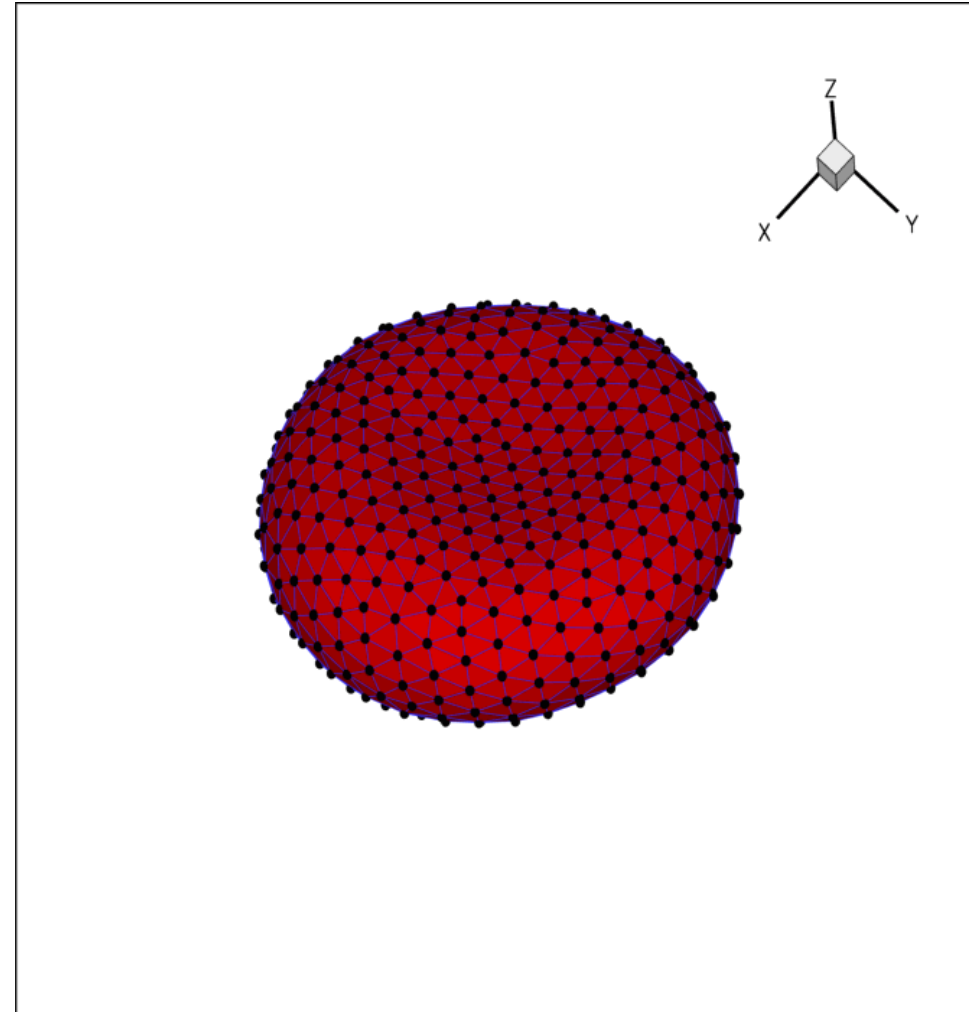
- No nucleus, organelles, and inner cytoskeleton
- Membrane: lipid bilayer with an attached spectrin network
- 50-100 nm spectrin length between junctions, 27000 – 40000 of junctions per RBC



# Membrane model

## Triangular network:

- 1) vertices – membrane particles
- 2) edges – viscoelastic springs
- 3) bending energy between faces
- 4) constant surface area (local or global)
- 5) constant volume





# Deformation and dynamics of blood cells in microfluidics

# Microfluidics

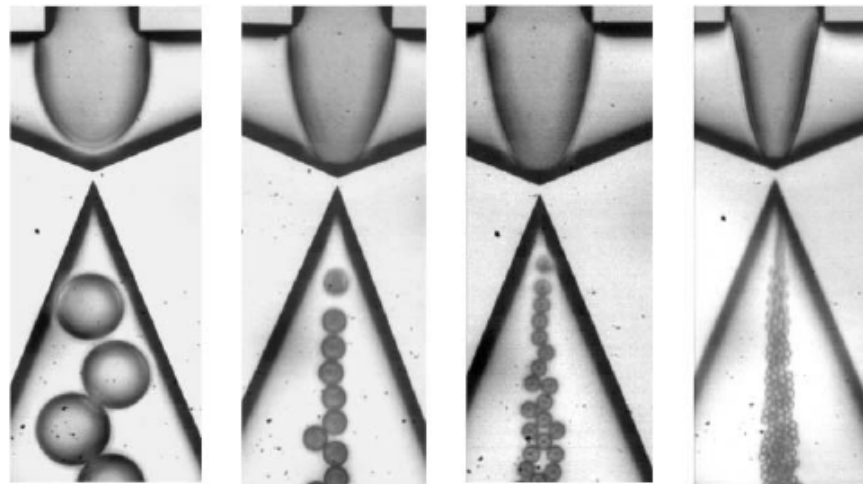
## Biomedical and engineering applications

Analysis and detection of suspended particles

Sorting and separation

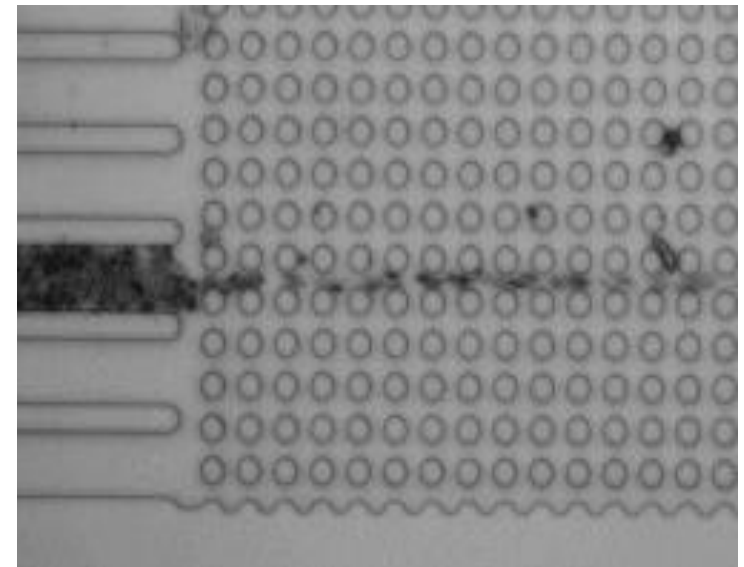
Manufacturing of micro-particles

### Droplet microfluidics



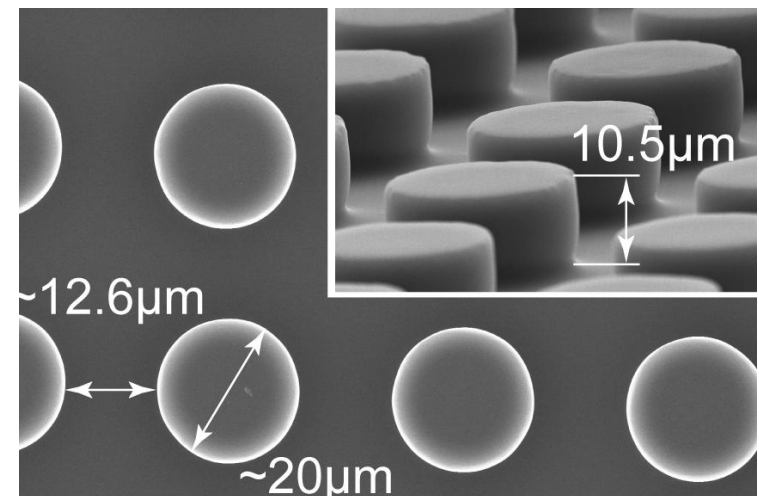
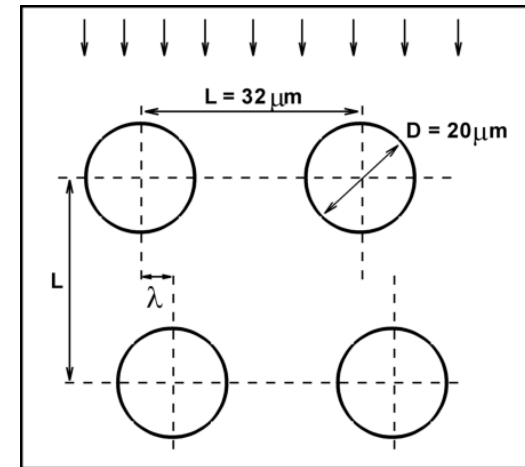
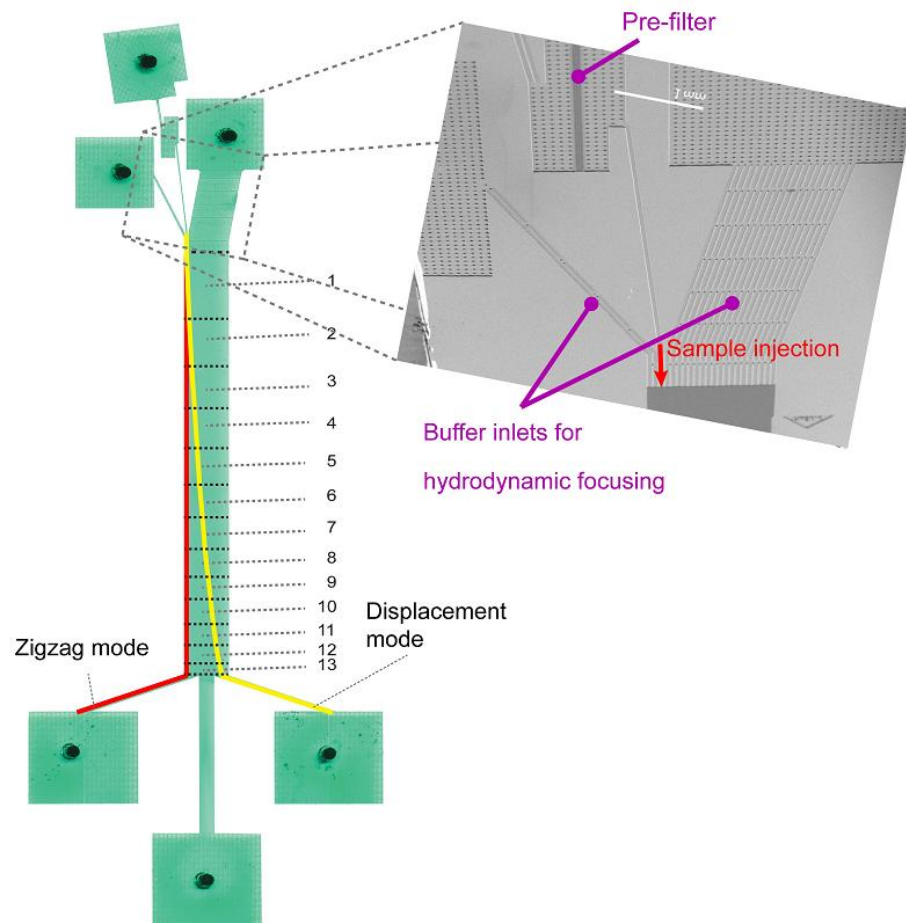
Yobas et al., *Lab Chip*, 6: 1073, 2006

### Bumper arrays



Holm et al., *Lab Chip*, 11: 1326, 2011

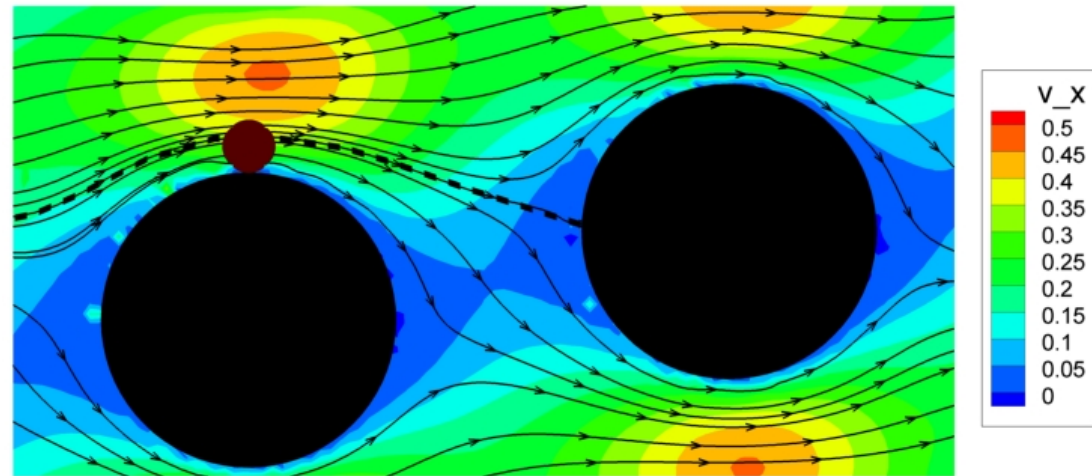
# Deterministic Lateral Displacement (DLD) Devices



# Basic principle of DLDs

DLD devices can be used efficiently for the separation of colloidal particles based on their size

Can we efficiently sort deformable particles (e.g., cells) in DLD devices?

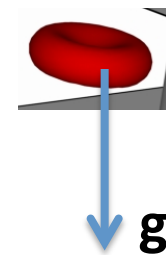
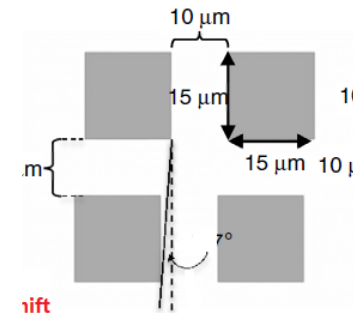
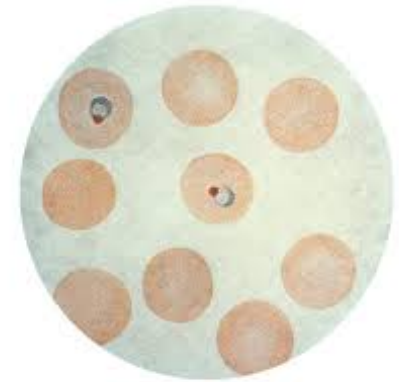


Understanding and optimization of obstacle array devices

European FP7 program: LAPASO - Label Free Particle Sorting

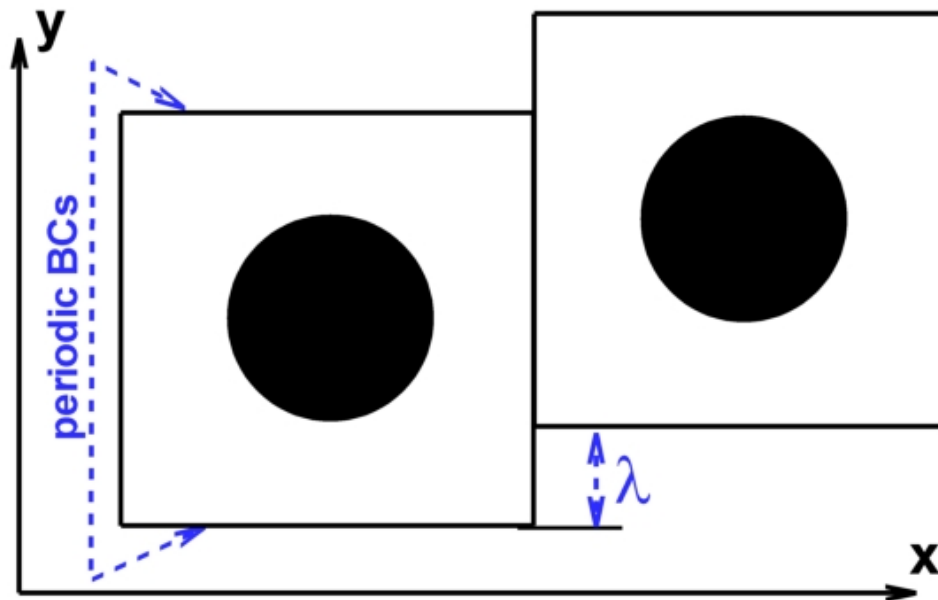
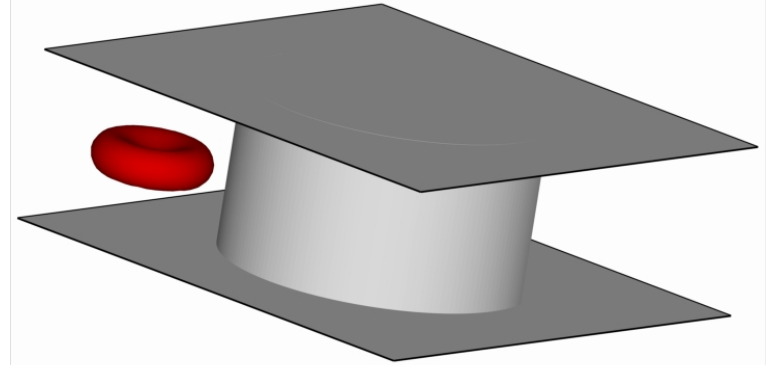
# Questions to address

- How sensitive is a DLD to the moderate changes of various RBC properties such as the cell size, membrane elasticity and bending rigidity, and the viscosity contrast?
- What geometrical configuration (e.g., pillar shape and size, their arrangement) of a DLD provides an 'optimal' performance?
- Can we improve the separation through the application of various external fields (e.g., gravity, dielectrophoresis, acoustophoresis)?



# Bumper array simulation

We are going to simulate only a single bumper!



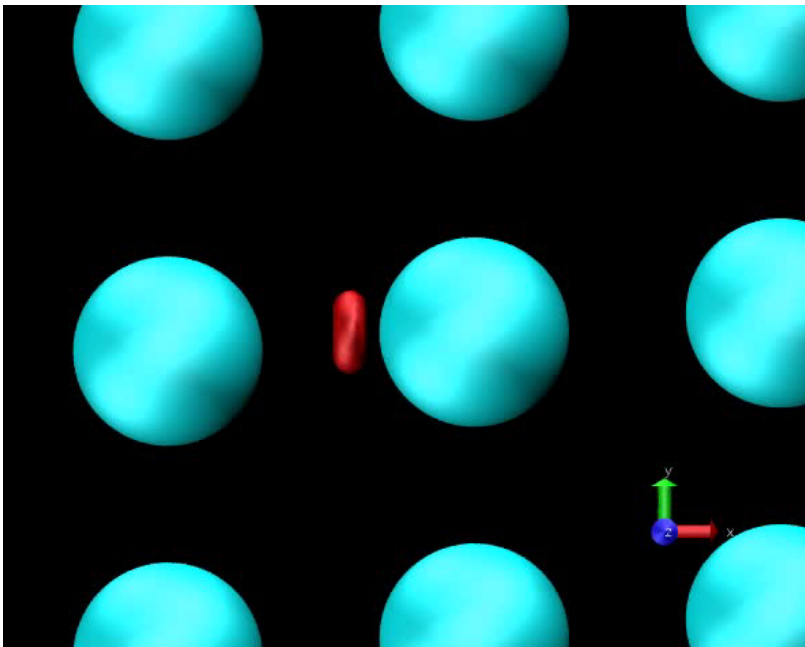
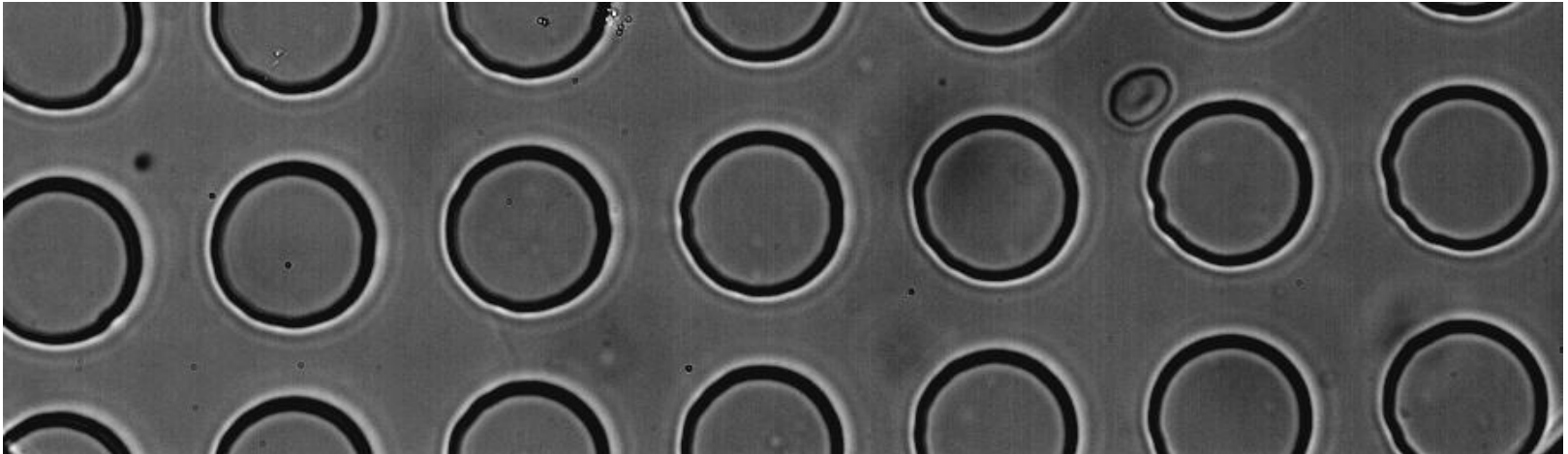
## Boundary conditions:

**X** – similar to Lees-Edwards BCs with the shift  $\lambda$ .

**Y** – periodic BCs.

**Z** – solid BCs.

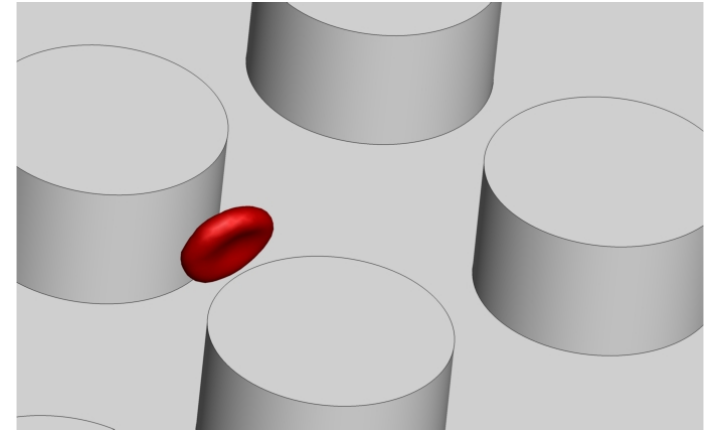
# Experiments & simulations



Section 4 of the device  
with the shift of 2 micron

# Summary and conclusions

- Bumper arrays can exploit cell size, shape, and deformability for sorting and detection
- Simulations allow us to observe in detail the cell dynamics, deformation, and orientation within the microfluidic device
- Microfluidics simulations can aid in the design of efficient micro-devices

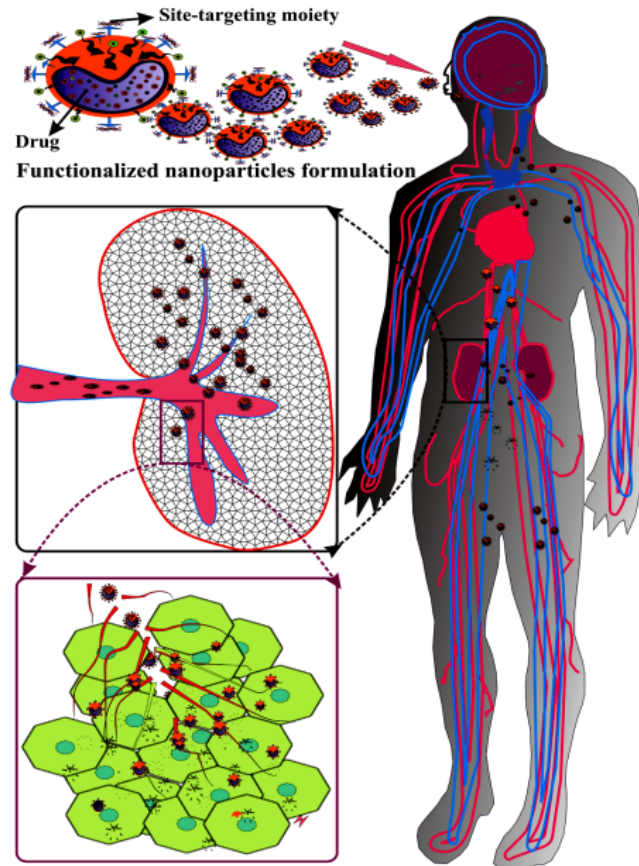




# Margination of micro- and nano-particles in blood flow

# Targeted drug delivery

## Drug delivery by micro- and nano-particles

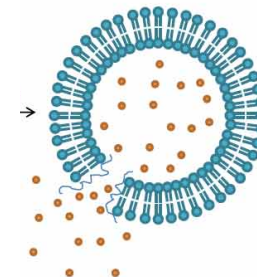
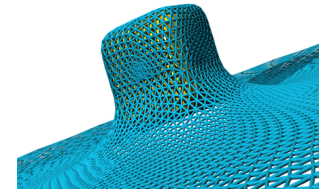
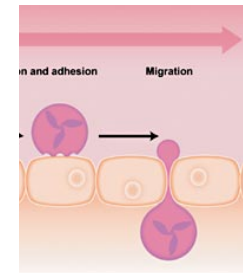
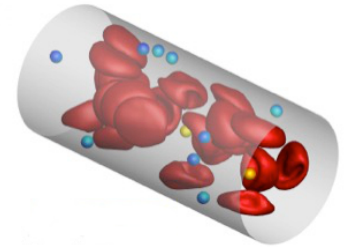
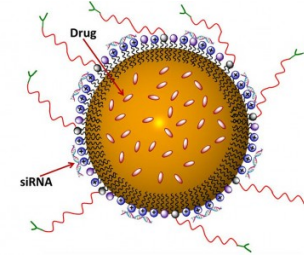


An idea of targeted drug delivery is very simple:

- i) Encapsulate drugs into “fully-functional” and “target-oriented” carriers
- ii) Administer the carriers into human body
- iii) Let the particles get delivered to specific targets
- iv) Release drugs at the targeted sites

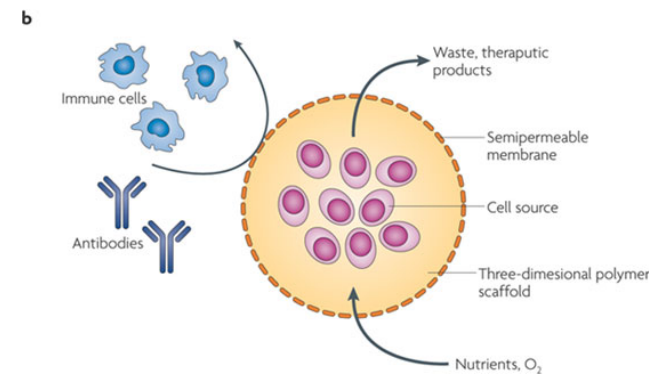
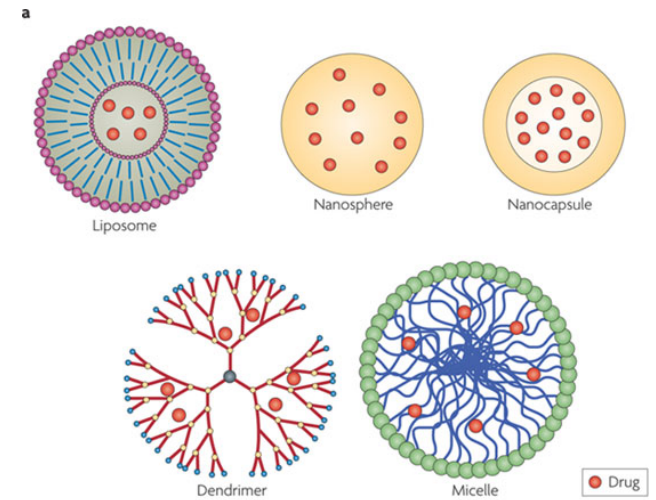
# Realization steps of drug delivery

- 1) Fabrication of micro- and/or nano-particles  
.....
- 2) Transport of the particles through a cardiovascular system  
.....
- 3) Transmigration of the particles through vascular walls and interstitial space  
.....
- 4) Particle uptake by cells and their transport within a cell  
.....
- 5) Release of drugs after a target has been reached



# Properties of drug carriers

- Various sizes (from several nanometers to a few micrometers)
- Different shapes (e.g., sphere, ellipsoid, disk, rod-like)
- Different composition (e.g., polymers, lipids)
- Various functionalities (e.g., receptors, break-up, stealth properties)
- Multistage drug carriers
- .....

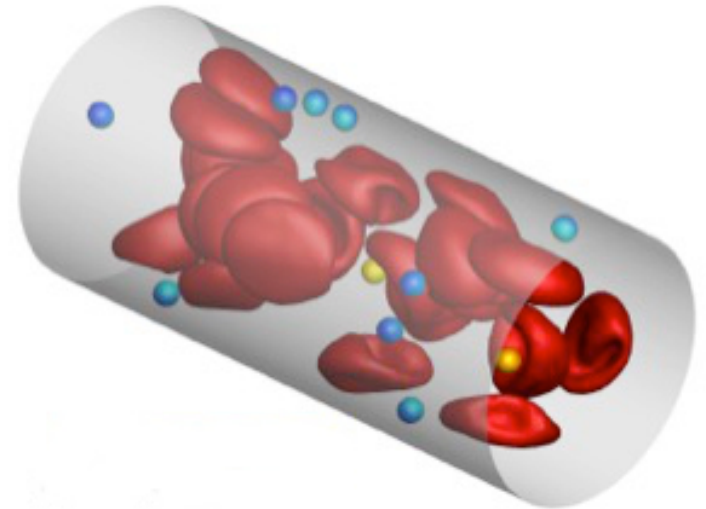


Nature Reviews | Neuroscience

Orive et al., *Nat. Rev. Neurosci.*,  
10:682, 2009

# Vascular drug delivery

- Particle transport through vascular networks
- Interactions with other blood cells
- Adhesion to vascular endothelium



## Questions:

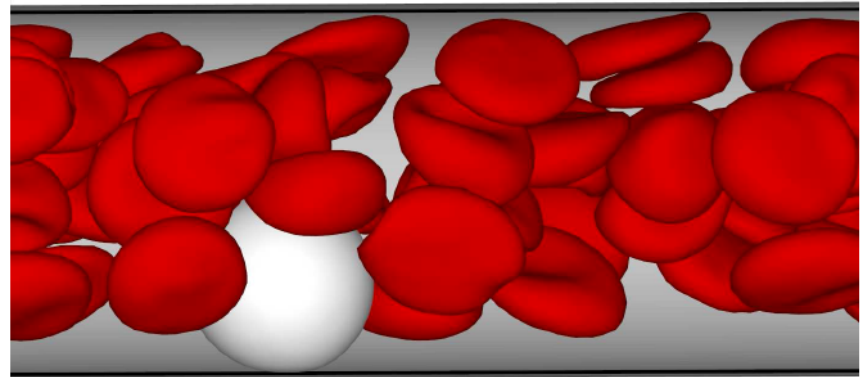
Müller et al., *Sci. Rep.*, 4:4871, 2014

- Effect of various blood flow conditions (e.g., flow rate, blood cell concentration) on the transport of particles
- Dependence of the transport on particle properties such as size, shape, deformability
- Interactions with other blood cells
- Adhesion to vascular endothelium

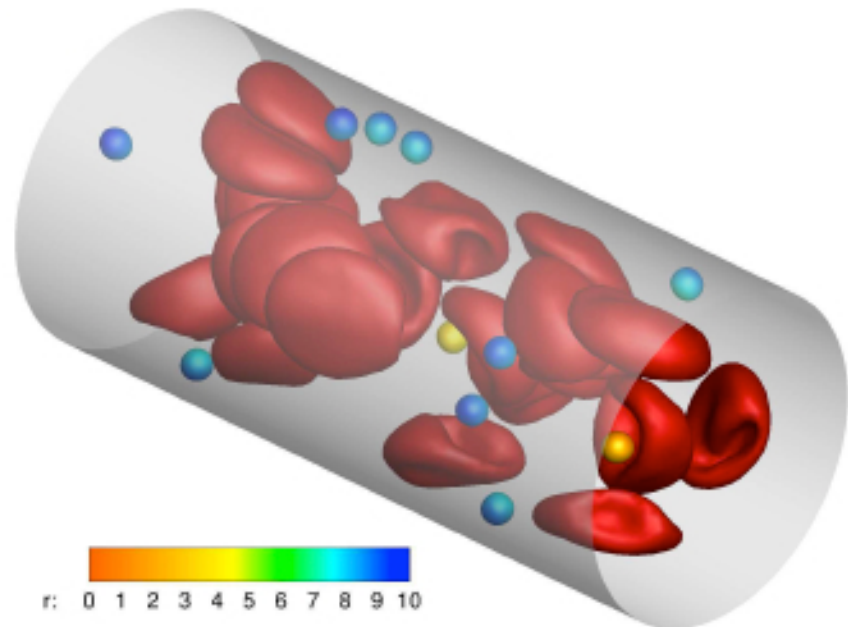
# Particle margination

Margination of particles and cells in blood flow

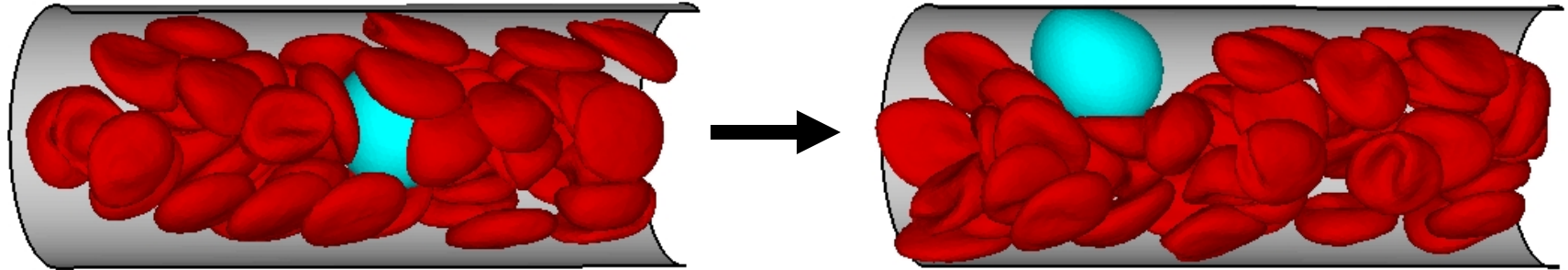
- white blood cells and platelets



- drug delivery carriers

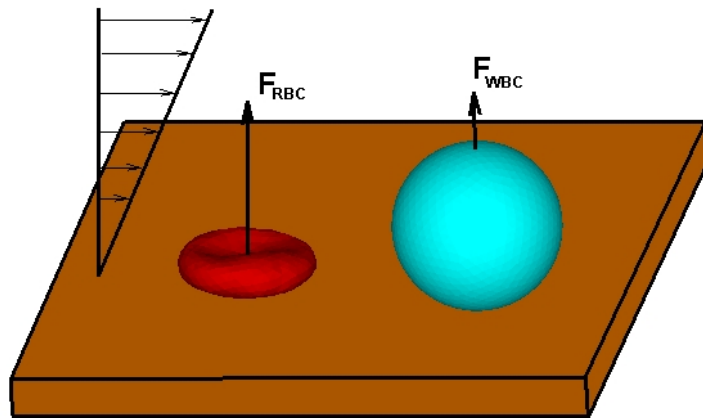


# Margination mechanisms



**Physical mechanisms and important factors?**

“Lift” force?



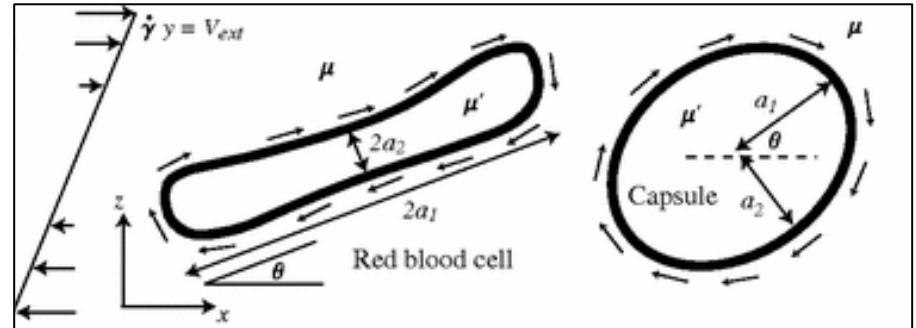
Shear induced diffusion or cell “collisions”?

**Contributing factors:** Hematocrit, RBC aggregation, cell properties, flow rate and geometry

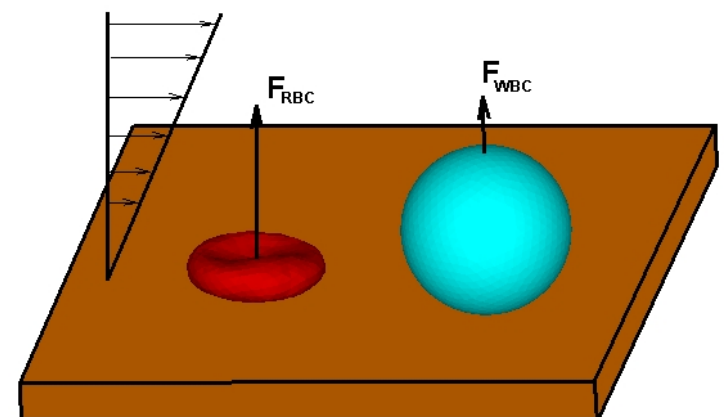
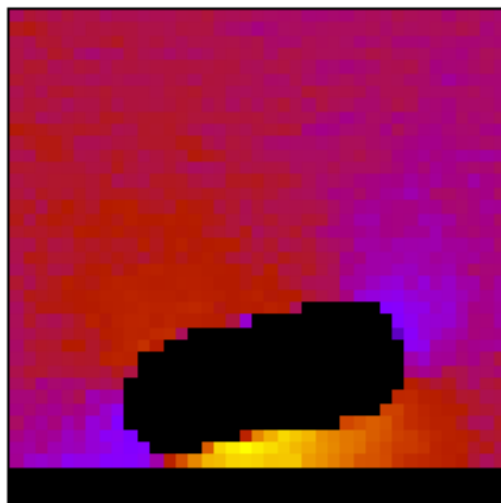
# Lift force

## Due to hydrodynamic interactions of cells with a wall

- RBC alignment in flow
- tank-treading motion of a membrane
- pressure difference



Skotheim & Secomb, *Phys. Rev. Lett.*, 98:078301, 2007



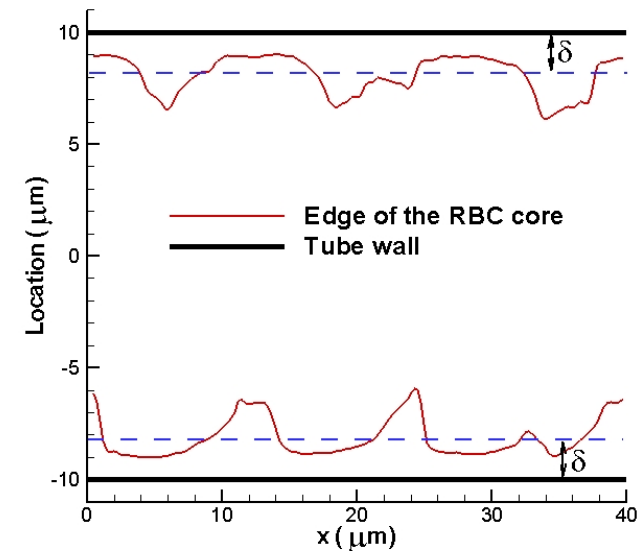
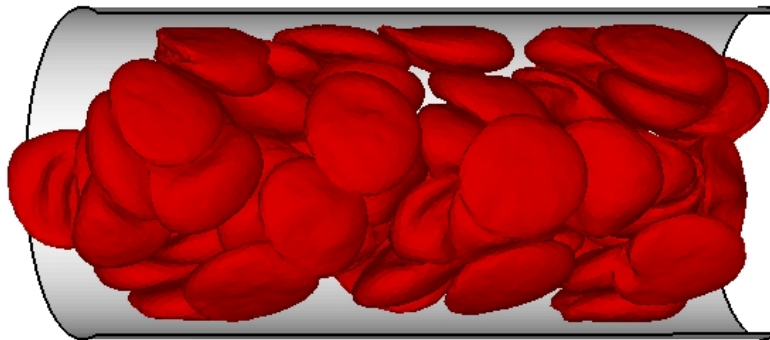
Messlinger et al., *Phys. Rev. E*, 80:011901, 2009



# RBC free layer

Lift force on RBCs leads to a layer next to a wall void of RBCs

## RBC-free layer (RBCFL)

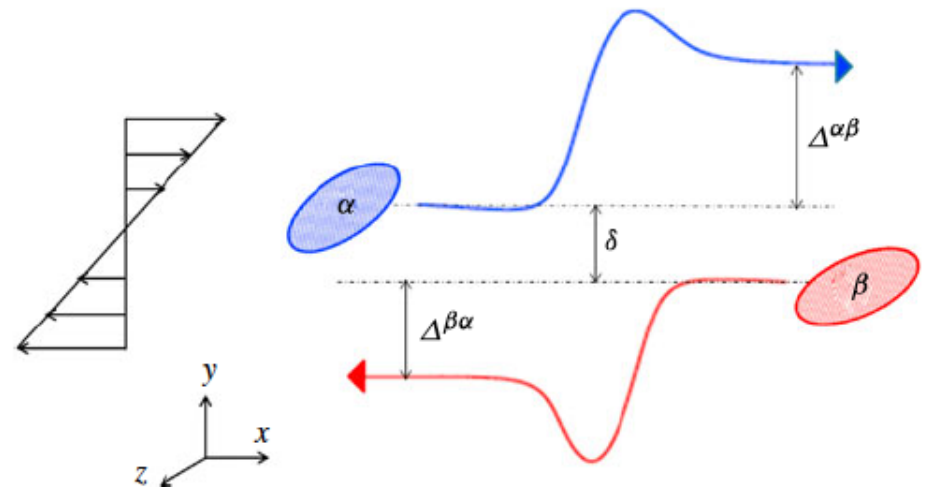
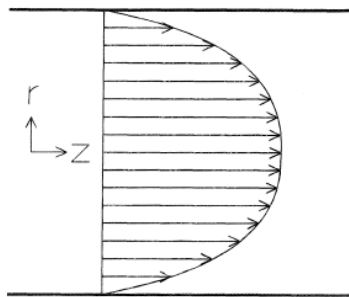


- RBCs migrate to the center of the tube forming a flow core
- Near the wall a RBC-free layer is formed absent of RBCs

# Shear-induced diffusion

Effective particle diffusion may be enhanced due to ‘collisions’ with RBCs

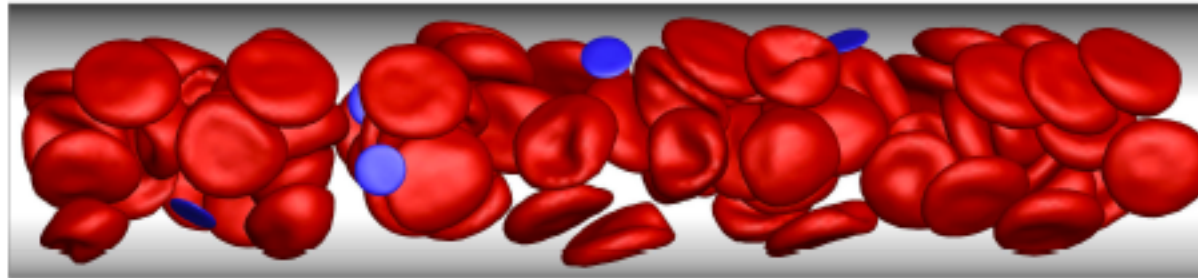
- Interactions of particles with RBCs lead to their enhanced diffusion
- Particle diffusion is non-uniform



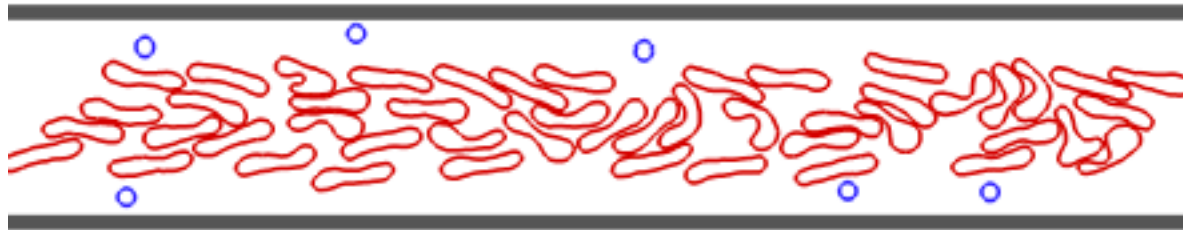
Kumar & Graham, *Phys. Rev. Lett.*, 109:108102, 2012

**A gradient in the effective diffusivity leads to particle drift!**

# Simulation system



- 3D

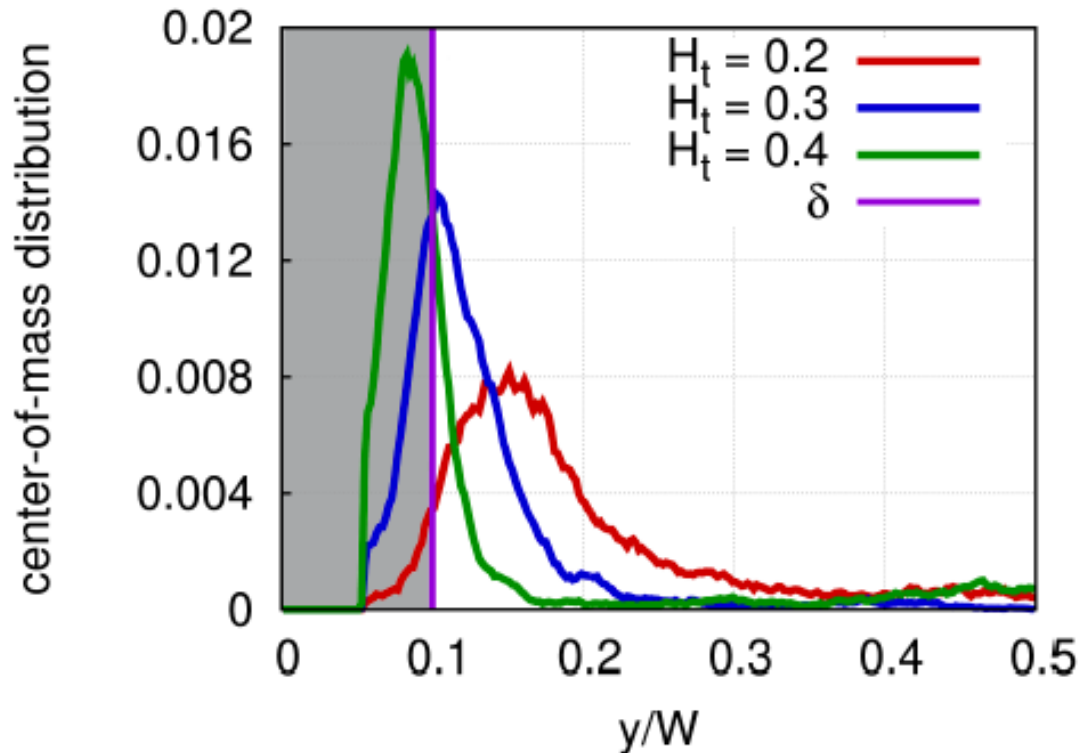


- 2D

## Characterized by:

- hematocrit  $H_t$
- non-dimensional shear rate  $\dot{\gamma}^* = \bar{\dot{\gamma}} \tau = \frac{\bar{v}}{W} \frac{\eta D_r^3}{\kappa}$
- particle size  $D_p$  and shape (spherical and ellipsoidal)

# Particle distribution

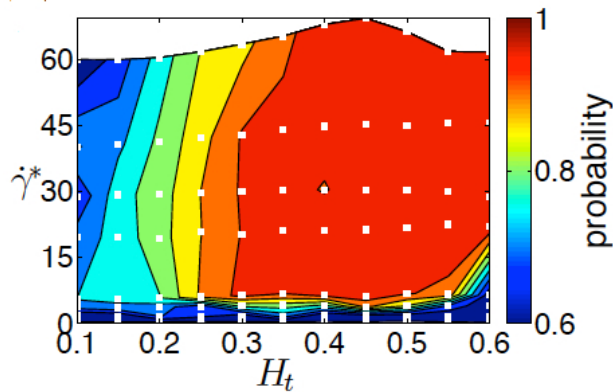


**Margination probability** is defined as a probability for a particle center of mass to be within the distance  $\delta$  away from the wall.

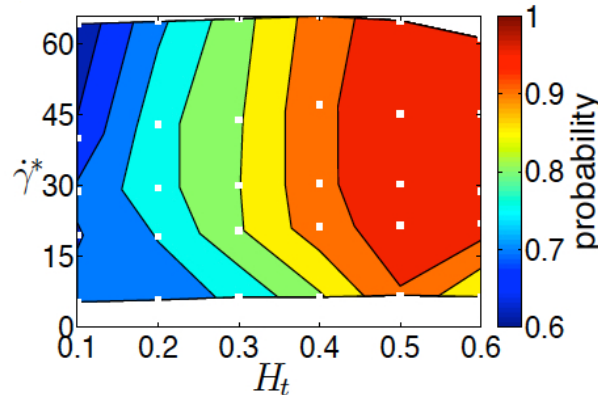
## Different choices of $\delta$ :

- RBC free layer, defined by the edge of RBC core
- $\delta$  = a fixed distance
- $\delta = D_p/2 + r$ , a distance  $r$  between the wall and particle surface

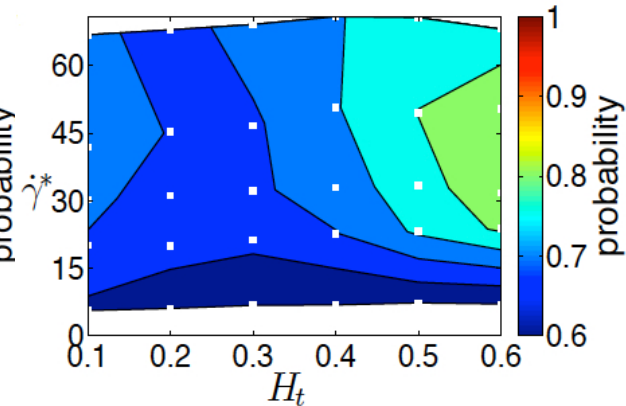
# Margination of particles with different sizes



$D_p = 0.3D_r$  (1.83  $\mu\text{m}$ )



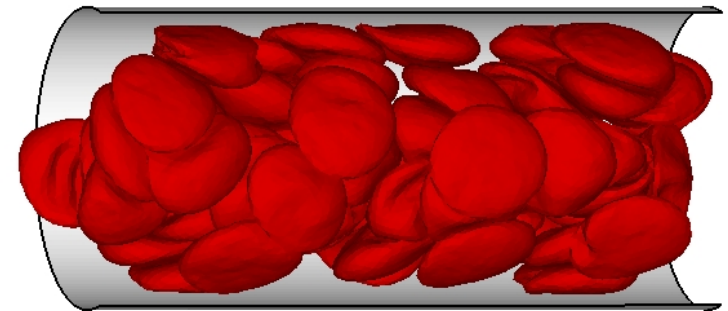
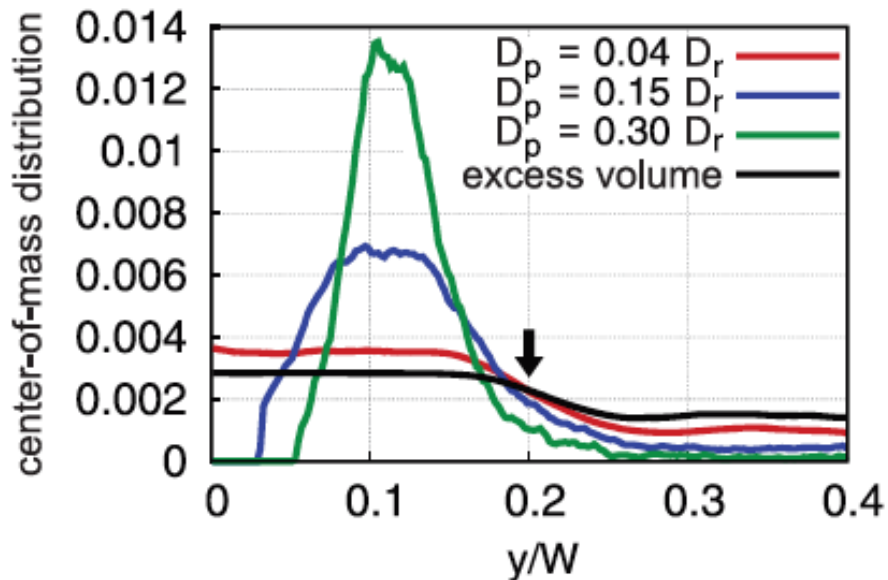
$D_p = 0.15D_r$  (0.91  $\mu\text{m}$ )



$D_p = 0.04D_r$  (0.25  $\mu\text{m}$ )

- particle margination probability is based on the RBCFL thickness
- particle margination worsens as the particle becomes smaller
- margination of particles with a  $D_p$  smaller than about 200 nm can be described well by the distribution of blood plasma

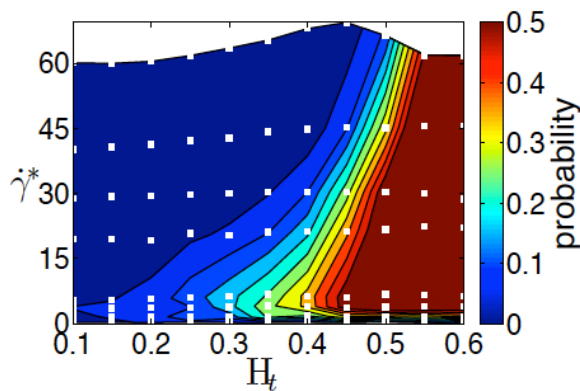
# Distribution of small nano-particles



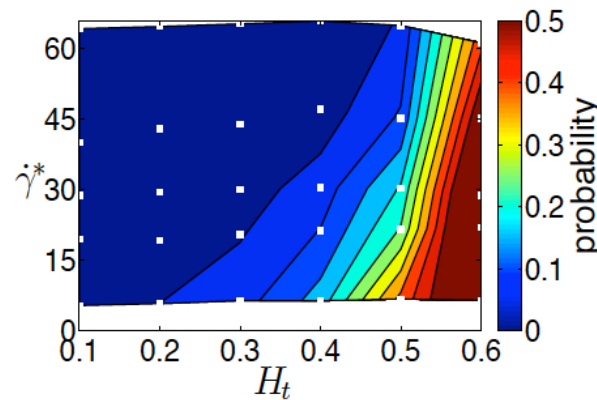
Margination of particles with a  $D_p$  smaller than about 200 nm can be described well by the distribution of blood plasma

# Margination into the potential adhesion layer

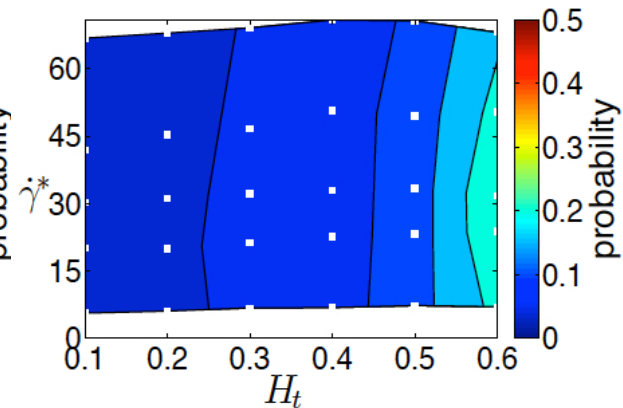
Potential adhesion layer  $\approx 200$  nm  $\Rightarrow \delta = D_p/2 + 200$  nm



$D_p = 0.3 D_r$  ( $1.83 \mu\text{m}$ )



$D_p = 0.15 D_r$  ( $0.91 \mu\text{m}$ )

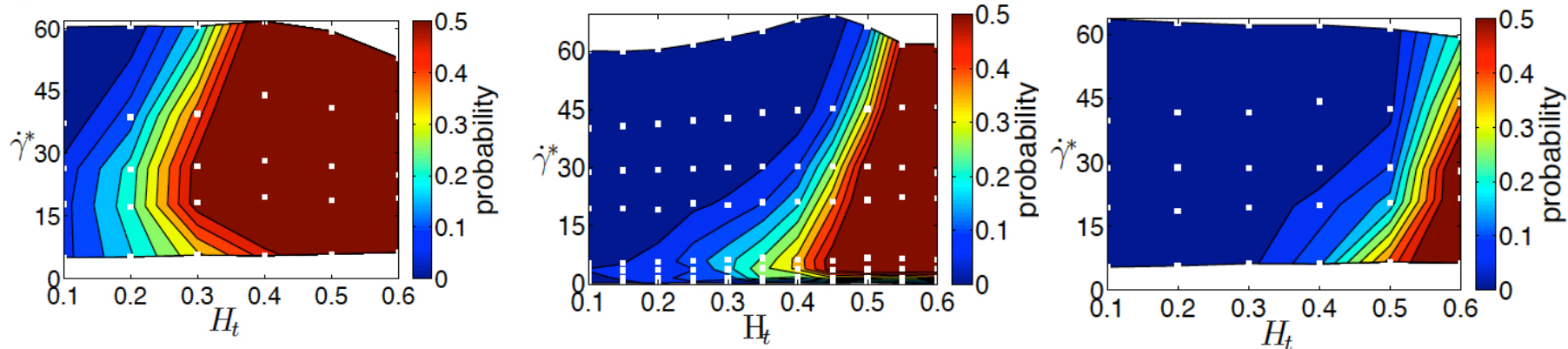


$D_p = 0.04 D_r$  ( $0.25 \mu\text{m}$ )

Particle margination into the potential adhesion layer worsens as the particle becomes smaller

# Effect of vessel diameter on particle margination

Potential adhesion layer  $\approx 200$  nm  $\Rightarrow \delta = D_p/2 + 200$  nm



$W = 10 \mu\text{m}$

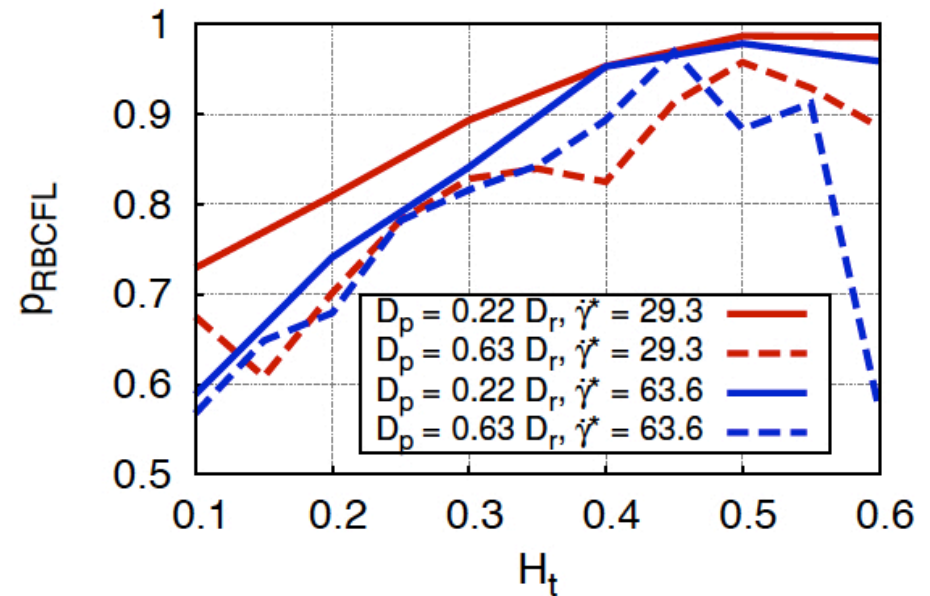
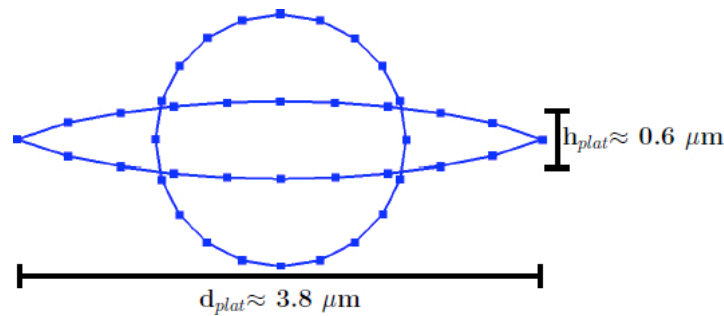
$W = 20 \mu\text{m}$

$W = 40 \mu\text{m}$

- particle margination into the potential adhesion layer with  $\delta = D_p/2 + 200$  nm and for  $D_p = 0.3D_r$  ( $1.83 \mu\text{m}$ )
- margination worsens as the vessel diameter is increased
- particle adhesion is mainly expected in small vessels



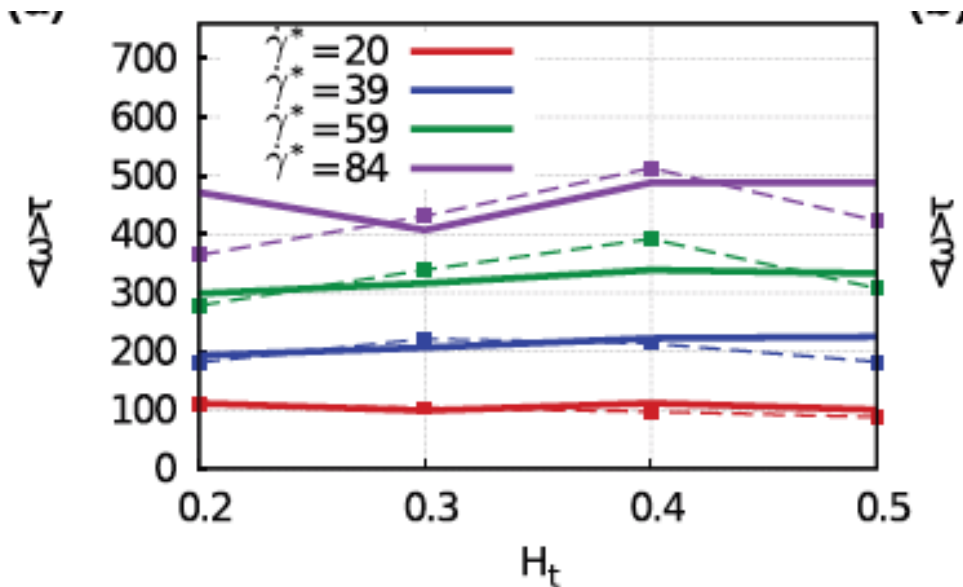
# Margination of particles with different shapes



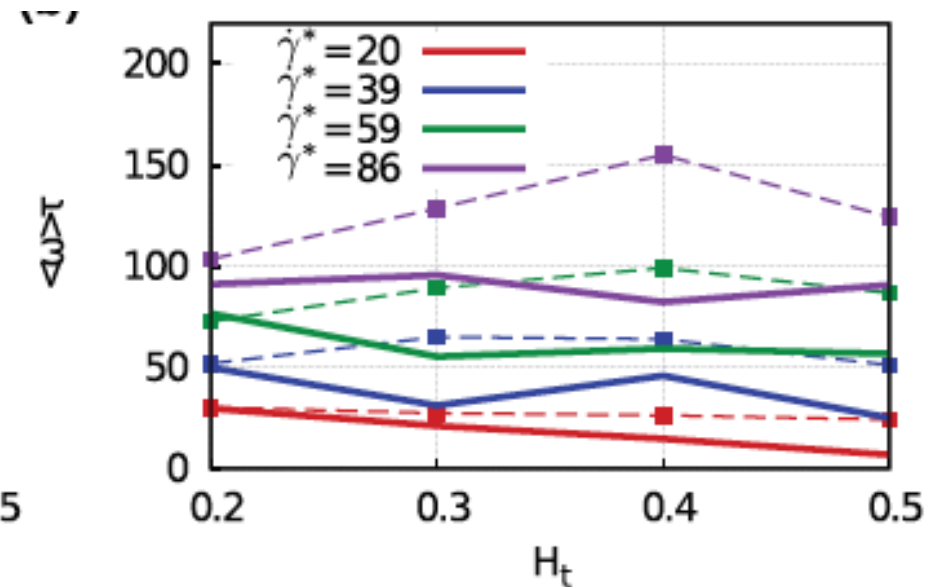
Ellipsoidal particles marginate slightly worse than spherical particles

# Particle dynamics in the RBCFL

## Sphere



## Ellipsoid



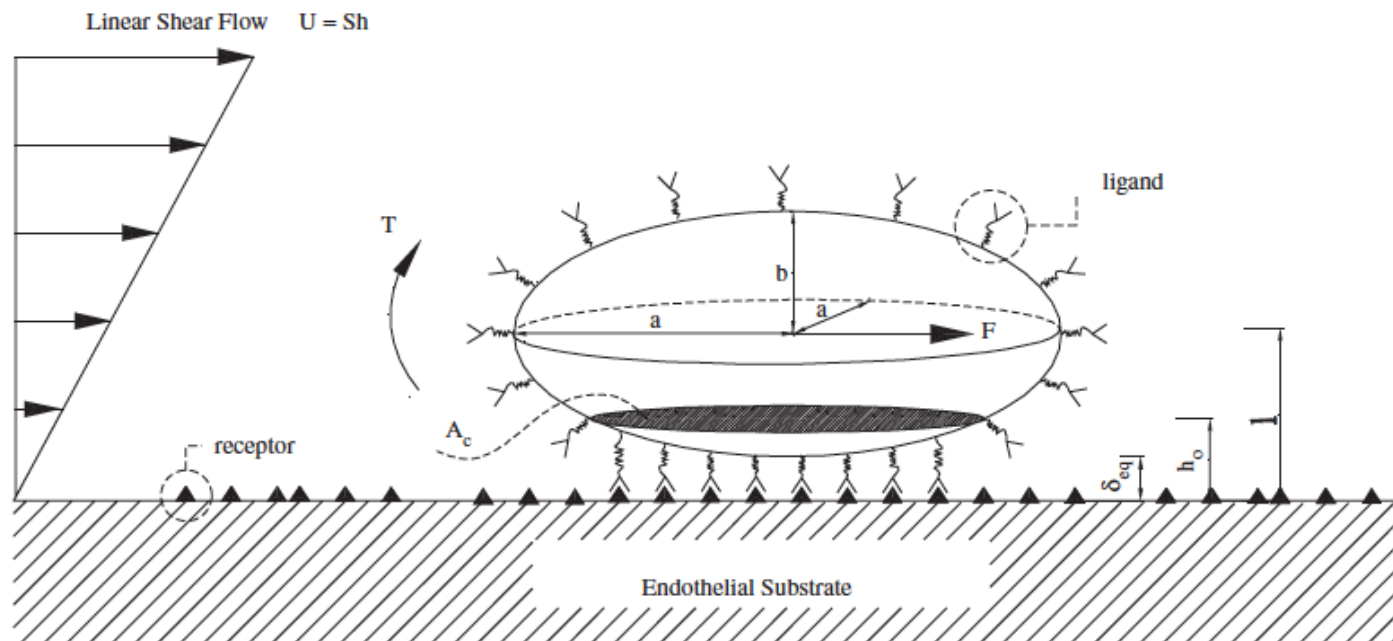
Jeffery prediction in shear flow:

$$\langle \omega \rangle = \frac{\dot{\gamma}}{r_e + 1/r_e}$$

Rotation (tumbling) of marginated ellipsoids within the RBCFL is slower than that of spheres leading to a longer interaction with a wall

# Particle adhesion

- Ellipsoidal particles adhere stronger than the spherical ones due to a larger area for particle-wall interaction
- Ellipsoidal particles rotate slower within the RBCFL
- Drag force on an adhered ellipsoidal particle appears to be smaller than on a spherical one having the same volume

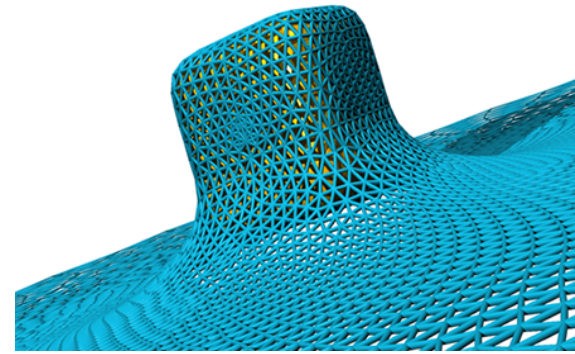


Decuzzi & Ferrari, *Biomaterials*, 27:5307, 2006

# “Best” particle properties?

From the point of view of particle margination in blood flow the best particles for drug delivery are micron size ellipsoidal particles rather than spherical nanometer size particles.

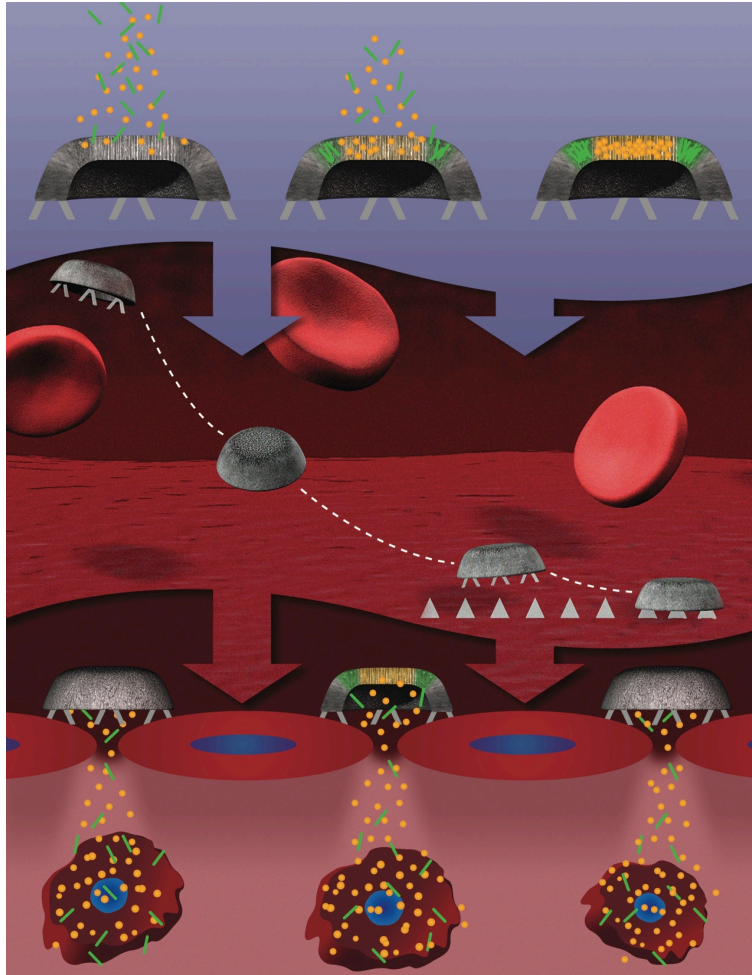
However, what particle properties are best for their transport through vascular walls and interstitial space, and their uptake by cells?



Dasgupta et al., *Nano Lett.*, 14:687, 2014

**As a conclusion, we need to integrate the knowledge about particle performance at various drug delivery steps in order to decide on the optimal particle properties.**

# Multistage delivery systems



- May change their size at different stages of the drug delivery process
- Perform multiple tasks at different stages
- May include a number of different targets

## Other ideas:

- active particles
- external forces
- ....

# Summary and conclusions

- ❖ Larger particles (micron size) possess better margination properties than sub-micron particles
- ❖ Adhesion of drug carriers is mainly expected in small vessels
- ❖ Ellipsoidal particles are expected to adhere better due to slower rotational dynamics within the RBCFL and a larger area for adhesion
- ❖ From the vascular drug-delivery standpoint, ellipsoidal micron-size particles are likely to be advantageous for drug delivery
- ❖ However, an optimal strategy for drug delivery requires integration of the knowledge about particle performance at different delivery stages

# Acknowledgements

## PhD students:

Dinar Katanov  
Johannes Mauer  
**Ewan Henry**  
Masoud Hoore

## Postdocs:

**Kathrin Müller**  
Davod Alizadehrad  
**Zunmin Zhang**

## Collaborators:

**Forschungszentrum Jülich (Germany):**

Gerhard Gompper, Roland Winkler, Thorsten Auth

**Lund University (Sweden):**

**Stefan Holm, Jason Beech, Jonas Tegenfeldt**

**Institut Curie (France):**

Herve Turlier, Timo Betz, Jean-Francois Joanny



**Alexander von Humboldt**  
Stiftung/Foundation



# Jülich Supercomputing Centre (JSC)